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# Motivation



Signature schemes strike a balance between:

- Sizes (verification key and signatures)
- ✤ Speed (signing, verification)
- 🏨 Portability
- Conservative assumptions
- 💖 Resistance against side-channel attacks

And so on...

Criteria	1	*	1	<b>&gt;</b>	<b>~</b>
Dilithium	**1	***	***	**	•
Falcon	***	***	**	**	6
SPHINCS+	*1	**	**	***	67
Raccoon	**	***	***	**	***



# Side-channel attacks in cryptography





Timing measurement [Koc96]



Electromagnetic emissions [Eck85]



Acoustic emissions [AA04]





In Falcon, a signature **sig** is distributed as a Gaussian.

The signing key **sk** should remain private.

The power consumption leaks information about the dot product  $\langle sig, sk \rangle$ , or sk itself.



Figure 1: Flowchart of the signature

<sup>1</sup>FALCON Down: Breaking FALCON Post-Quantum Signature Scheme through Side-Channel Attacks [KA21]

**"SHIELD** 

In Falcon, a signature  ${\bf sig}$  is distributed as a Gaussian.

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Figure 1: Flowchart of the signature

<sup>2</sup>Improved Power Analysis Attacks on Falcon [ZLYW23]



## t-probing model

Adversary can probe t circuit values at runtime
 Unrealistic but a good starting point

#### Masking

Lach sensitive value x is split in *d* shares:

$$[\![x]\!] = (x_0, x_1, \dots, x_{d-1}) \tag{1}$$

such that

$$x_0 + x_1 + \dots + x_{d-1} = x \tag{2}$$

In t-probing model, ideally 0 leakage if d > t
 In "real life", security is exponential in d
 What about computations?







#### Remember this puzzle?

" A farmer with a wolf, a goat, and a cabbage must cross a river by boat. The boat can carry only the farmer and a single item. If left unattended together, the wolf would eat the goat, or the goat would eat the cabbage. How can they cross the river without anything being eaten? "



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#### Remember this puzzle?

" A farmer with a wolf, a goat, and a cabbage must cross a river by boat. The boat can carry only the farmer and a single item. If left unattended together, the wolf would eat the goat, or the goat would eat the cabbage. How can they cross the river without anything being eaten? "





It gets quickly complicated...

Now replace:

- **1** The set { farmer, wolf, goat, cabbage } by the shares  $(x_0, \ldots, x_{d-1})$
- 2 The operation "everyone crosses the river" by an arbitrary function  $f([x]) \rightarrow [y]$
- 3 The constraints "never leave A alone with B" by "a probing adversary shall not learn anything"
- ... and you obtain an inexhaustible source of headaches for cryptographers.

### How difficult are operations to mask?

- Addition ([[c]] = [[a + b]])?
   Compute [[c]] = (a<sub>0</sub> + b<sub>0</sub>,..., a<sub>d-1</sub> + b<sub>d-1</sub>), simple and fast: Θ(d) operations
   Multiplication ([[c]] = [[a ⋅ b]])?
   Complex and slower: Θ(d<sup>2</sup>) operations
   More complex operations?
  - > Use so-called mask conversions, very slow:  $\gg \Theta(d^2)$  operations



# **PSHIELD**

#### $\mathsf{Keygen}(1^{\lambda}) \to (\mathsf{sk}, \mathsf{vk})$

**1** Generate a large matrix  $\mathbf{A} = [\mathbf{I} | \bar{\mathbf{A}}] \in \mathcal{R}_q^{k \times (k+\ell)}$ 

- 2 Generate a short secret s
- Ompute t = A ⋅ s
- 4 Verification key vk = (A, t)

⊳ No mask

⊳ Slow

⊳ Fast

⊳ No mask

⊳ No mask

When masking this algorithm, the bottleneck is sampling **s** (2):

- ightarrow Concretely, start with boolean masking, then apply B2A conversions
- → Total masking overhead:  $O(d^2 \log q)$





We show that **s** retains a large amount of randomness **even in the presence of a probing adversary**.



Dilithium follows the Fiat-Shamir with aborts paradigm.

Sign(sk = s, vk = s)	$(\textbf{A},\textbf{t}), \textsf{msg}) \rightarrow \textsf{sig}$
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- 1 Generate a short ephemeral secret **r**
- 2 Compute the commitment  $\mathbf{w} = \mathbf{A} \cdot \mathbf{r}$
- **6** Compute the challenge  $c = H(\mathbf{w}, \mathsf{msg}, \mathsf{vk})$
- 4 Compute the response  $\mathbf{z} = \mathbf{s} \cdot \mathbf{c} + \mathbf{r}$
- **6** Check that **z** is in a given interval. If not, restart.
- **6** Signature is  $sig = (c, \mathbf{z})$

#### Masking bottlenecks:

- 69 Short secret generation (1) requires B2A.
- Rejection sampling (5) requires A2B and B2A.

Total masking overhead:  $\Theta(d^2 \log q)$ 

⊳ Slow

⊳ Fast

⊳ No mask

⊳ Fast

⊳ Slow

#### $\mathsf{Sign}(\mathsf{sk} = [\![ \textbf{s} ]\!], \mathsf{vk} = (\textbf{A}, \textbf{t}), \mathsf{msg}) \to \mathsf{sig}$

- Generate a masked short ephemeral secret **[r]** using "AddRepNoise" ▷ Fast
- **2** Compute the commitment  $[w] = A \cdot [r]$
- 🔞 Unmask [**[w**]] to obtain **w**
- Compute the challenge  $c = H(\mathbf{w}, \mathsf{msg}, \mathsf{vk})$
- **6** Compute the response  $[\mathbf{z}] = [\mathbf{s}] \cdot c + [\mathbf{r}]$
- 🙆 Unmask [[**z**]] to obtain **z**
- (No more rejection sampling!)

```
8 Signature is sig = (c, \mathbf{z})
```

Total masking overhead:  $O(d \log d)$ 

▷ Fast▷ Fast

⊳ No mask

⊳ Fast

⊳ Fast



# Impact on the modulus





## Impact on the modulus



 $m{0}$  Removing rejection sampling increases  $\|m{r}\|/\|m{s}\|$  from  $\Theta(\dimm{s})$  to  $\Theta\left(\|c\|\sqrt{ ext{Queries}}
ight)$ 

# Impact on the modulus



Removing rejection sampling increases ||r||/||s|| from Θ(dim s) to Θ (||c||√Queries)
 The increased q in turn requires increasing ||s||, q/||r|| and/or the dimensions.







Raccoon is a specific-purpose scheme aimed at high side-channel resistance:

- ☺ Same assumptions as Dilithium
- 🙂 Simpler
- Verification key size is similar
- 😟 Signature is 4x larger
- (2) When masked, orders of magnitude faster than other schemes are





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