Masking-Friendly Signatures and the Design of Raccoon

Rafael del Pino PQShield Thomas Espitau PQShield Shuichi Katsumata PQShield AIST

Mary Maller POShield

Ethereum Foundation

Fabrice Mouhartem CryptPad <u>Thomas Prest</u> PQShield

Markku-Juhani Saarinen

PQShield Tampere University

Mélissa Rossi ANSSI



Signature schemes strike a balance between:

- Sizes (verification key and signatures)
- Speed (signing, verification)
- 🏨 Portability
- Conservative assumptions
- 💖 Resistance against side-channel attacks

And so on...







Side-channel attacks in cryptography





Timing measurement [Koc96]



Electromagnetic emissions [Eck85]



Acoustic emissions [AA04]





In Falcon, a signature **sig** is distributed as a Gaussian.

The signing key **sk** should remain private.

The power consumption leaks information about the dot product $\langle sig, sk \rangle$, or sk itself.



Figure 1: Flowchart of the signature

¹FALCON Down: Breaking FALCON Post-Quantum Signature Scheme through Side-Channel Attacks [KA21]

P[®]SHIELD

In Falcon, a signature ${\bf sig}$ is distributed as a Gaussian.

The signing key **sk** should remain private.

The power consumption leaks information about the dot product (sig, sk), or sk itself.





Figure 1: Flowchart of the signature

²Improved Power Analysis Attacks on Falcon [ZLYW23]

t-probing model

Adversary can probe t circuit values at runtime
 Unrealistic but a good starting point

Masking

Lach sensitive value x is split in d shares:

$$[\![x]\!] = (x_0, x_1, \dots, x_{d-1}) \tag{1}$$

such that

$$x_0 + x_1 + \dots + x_{d-1} = x \tag{2}$$

In t-probing model, ideally 0 leakage if d > t
 In "real life", security is exponential in d
 What about computations?





Remember this puzzle?

" A farmer with a wolf, a goat, and a cabbage must cross a river by boat. The boat can carry only the farmer and a single item. If left unattended together, the wolf would eat the goat, or the goat would eat the cabbage. How can they cross the river without anything being eaten? "



"SHIELD

Remember this puzzle?

" A farmer with a wolf, a goat, and a cabbage must cross a river by boat. The boat can carry only the farmer and a single item. If left unattended together, the wolf would eat the goat, or the goat would eat the cabbage. How can they cross the river without anything being eaten? "





It gets quickly complicated...

Now replace:

- **1** The set { farmer, wolf, goat, cabbage } by the shares (x_0, \ldots, x_{d-1})
- 2 The operation "everyone crosses the river" by an arbitrary function $f([x]) \rightarrow [y]$
- 3 The constraints "never leave A alone with B" by "a probing adversary shall not learn anything"

... and you obtain an inexhaustible source of headaches for cryptographers.

Now replace:

- **1** The set { farmer, wolf, goat, cabbage } by the shares (x_0, \ldots, x_{d-1})
- 2 The operation "everyone crosses the river" by an arbitrary function $f(\llbracket x \rrbracket) \to \llbracket y \rrbracket$
- 3 The constraints "never leave A alone with B" by "a probing adversary shall not learn anything"

... and you obtain an inexhaustible source of headaches for cryptographers.

How difficult are operations to mask?

- **Goldstring (**[[c]] = [[a + b]]**)**?
 - Simple and fast: $\Theta(d)$ operations
- \bigcirc Refresh ($\llbracket a \rrbracket \rightarrow \llbracket a \rrbracket'$)?
 - Protect against attacks and allows composition frameworks (SNI, PINI, IOS, etc.)
 - Simple and fast: $\Theta(d \log d)$ operations
- \bigcirc Multiplication ($[c]] = [a \cdot b]$)?
 - > Complex and slower: $\Theta(d^2)$ operations

More complex operations?

> Use so-called mask conversions, very slow: $\Theta(d^2)$ operations **per bit to convert**



Dilithium-Sign

- **1** Sample $\mathbf{r} \leftarrow \text{Uniform}(S)$
- **2** w := Ar
- $\mathbf{3} \mathbf{w}_{\top} := [\mathbf{w}]_k$
- **5** z := s *c* + r
- 6 If **z** not in S', goto 1

$$\mathbf{0} \mathbf{h} := \mathbf{w}_{\top} - [\mathbf{A}\mathbf{z} - \mathbf{t}\mathbf{c}]$$

8 Output sig = $(c, \mathbf{z}, \mathbf{h})$

Masking Dilithium step-by-step

Pa SHIELD

(4)

(5)

Dilithium-Sign

- $\bigcirc Sample \mathbf{r} \leftarrow Uniform(S)$
- 2 w := A r
- $\mathbf{0} \mathbf{w}_{\mathsf{T}} := [\mathbf{w}]_k$
- **5 z** := **s** *c* + **r**
- 6 If **z** not in S', goto 1

$$\mathbf{0} \mathbf{h} := \mathbf{w}_{\top} - [\mathbf{A}\mathbf{z} - \mathbf{t}\mathbf{c}]_{I}$$

8 Output sig = $(c, \mathbf{z}, \mathbf{h})$

1 How do we sample a uniform *d*-sharing [r] of $r \leftarrow \text{Uniform}(S)$ securely?

- \Rightarrow $S = \mathbb{Z}_q^n$ is easy, $S \subsetneq \mathbb{Z}_q$ is hard
- \rightarrow Naive solutions do not work
- ➔ Best known method:
 - Find a **boolean** circuit *f* that samples $(r_1, ..., r_{\log q}) \leftarrow \text{Uniform}(S)$
 - 2 Evaluate *f* in masked boolean form:
 - $(\llbracket r_1 \rrbracket_b, \dots, \llbracket r_{\log q} \rrbracket_b) \leftarrow \llbracket f \rrbracket_b$ (3)
 - **3** Use mask conversion on each bit: $[[r_i]]_b \to [[r_i]]_a$
 - **Q** Recombine the masked bits: $\llbracket r \rrbracket_a := \sum_i 2^i \llbracket r_i \rrbracket_a$ Complexity: O (d² (|f| + log q))

Dilithium-Sign

- **1** Sample $\mathbf{r} \leftarrow \text{Uniform}(S)$
- 2 w := Ar

- **5** z := s c + r
- 6 If **z** not in S', goto 1

$$\mathbf{0} \mathbf{h} := \mathbf{w}_{\top} - [\mathbf{A}\mathbf{z} - \mathbf{t}c]_k$$

Output sig = (c, z, h)

2 Compute **Ar**:

- → Linear operation thus easy
- \rightarrow Complexity: $\tilde{O}(d)$

3 Bit dropping $\mathbf{w}_{\mathsf{T}} := [\mathbf{w}]_k$:

 \rightarrow The lower bits of **w** are sensitive:

$$\mathbf{w} - (\mathbf{A}\mathbf{z} - \mathbf{t}c) = \mathbf{e}c$$

- → Requires mask conversion (B2A + A2B)
- → Complexity: $O(d^2 \log q)$
- 4 Challenge computation is unmasked:
 - → Previously: ad-hoc assumption [BBE⁺18]
 - → Now: everyone cites [DFPS23]

PSHIELD

Dilithium-Sign

- **1** Sample $\mathbf{r} \leftarrow \text{Uniform}(S)$
- 2 w := Ar
- $\mathbf{0} \mathbf{w}_{\top} := \lfloor \mathbf{w} \rceil_k$
- **5** z := s c + r
- 6 If **z** not in *S*′, goto 1

$$\mathbf{0} \mathbf{h} := \mathbf{w}_{\top} - [\mathbf{A}\mathbf{z} - \mathbf{t}\mathbf{c}]_{I}$$

6 Compute $\mathbf{z} = \mathbf{s} c + \mathbf{r}$:

- → Linear thus fast
- 6 Rejection sampling:
 - \rightarrow Requires mask conversion (A2B), slow

Compute h:
 Linear thus fast

Masked Dilithium [CGTZ23]





Number of shares d

Masked Dilithium [CGTZ23]





Number of shares d

Masked Dilithium [CGTZ23]





Number of shares d

Takeaway



Masking Dilithium efficiently remains difficult despite several years of works:

- → Masking the GLP lattice-based signature scheme at any order [BBE⁺18]
- → Masking Dilithium efficient implementation and side-channel evaluation [MGTF19]
- Protecting dilithium against leakage: Revisited sensitivity analysis and improved implementations [ABC⁺23]
- → Improved Gadgets for the High-Order Masking of Dilithium [CGTZ23]

None of these works manage to break the $\Theta(d^2 \log q)$ barrier.

Takeaway



Masking Dilithium efficiently remains difficult despite several years of works:

- → Masking the GLP lattice-based signature scheme at any order [BBE⁺18]
- → Masking Dilithium efficient implementation and side-channel evaluation [MGTF19]
- Protecting dilithium against leakage: Revisited sensitivity analysis and improved implementations [ABC⁺23]
- → Improved Gadgets for the High-Order Masking of Dilithium [CGTZ23]

None of these works manage to break the $\Theta(d^2 \log q)$ barrier.

What about Mitaka?

- \rightarrow Last year: Mitaka: a simpler, parallelizable, maskable variant of Falcon [EFG+22]
- → Now: A Key-Recovery Attack against Mitaka in the t-Probing Model [Pre23]
 - Slides and video on https://tprest.github.io/

Mitaka cannot be masked efficiently with existing techniques.

Takeaway



Masking Dilithium efficiently remains difficult despite several years of works:

- → Masking the GLP lattice-based signature scheme at any order [BBE⁺18]
- → Masking Dilithium efficient implementation and side-channel evaluation [MGTF19]
- Protecting dilithium against leakage: Revisited sensitivity analysis and improved implementations [ABC⁺23]
- → Improved Gadgets for the High-Order Masking of Dilithium [CGTZ23]

None of these works manage to break the $\Theta(d^2 \log q)$ barrier.

What about Mitaka?

- → Last year: Mitaka: a simpler, parallelizable, maskable variant of Falcon [EFG+22]
- → Now: A Key-Recovery Attack against Mitaka in the t-Probing Model [Pre23]
 - Slides and video on https://tprest.github.io/

Mitaka cannot be masked efficiently with existing techniques.

Back to the drawing board!





- → We can completely deviate from existing schemes and frameworks
- Only hard constraints are security and masking-friendliness

















Solution: add refresh gadgets to separate the algorithm in independent layers Now a probing adversary learns at most (the sum of) *t* short noises.





Solution: add refresh gadgets to separate the algorithm in independent layers Now a probing adversary learns at most (the sum of) *t* short noises.

"Thomas, this is not a *t*-probing secure gadget!"



$\mathsf{Keygen}(1^{\lambda}) \to (\mathsf{sk}, \mathsf{vk})$

- **1** Generate $\mathbf{A} = [\mathbf{I} | \bar{\mathbf{A}}]$
- 2 Sample **[s**] using AddRepNoise
- **3** Compute $\mathbf{t} = \mathbf{A} \cdot [\![\mathbf{s}]\!]$
- ④ Unmask **[t**] to obtain t
- **6** Verification key is vk = (A, t)
- 6 Signing key is sk = **[s**]

Proof intuition:

 $\mathsf{LeakyKeygen}(1^{\lambda}) \to (\mathsf{sk}, \mathsf{vk}, \mathsf{aux})$

- **1** Generate $\mathbf{A} = [\mathbf{I} | \bar{\mathbf{A}}]$
- **2** $\mathbf{s}_0 \leftarrow \{\text{sum of } (\operatorname{rep} d t) \text{ short noises} \}$
- **3** Sample *t* short noises $(\bar{\mathbf{s}}_1, \ldots, \bar{\mathbf{s}}_t)$

$$\mathbf{4} \ \mathbf{s} := \mathbf{s}_0 + \sum_i \bar{\mathbf{s}}_i$$

- **5** t := A s
- $\label{eq:result} \begin{array}{l} \textbf{6} \\ \text{Return } vk = (\textbf{A}, \textbf{t}), \, sk = \textbf{s}, \, \text{auxiliary} \\ \text{information } \textbf{aux} = (\bar{\textbf{s}}_1, \dots, \bar{\textbf{s}}_t) \end{array}$
- → For any EUF-CMA t-probing adversary given access to Keygen (left alg.), we can construct an EUF-CMA adversary given access to LeakyKeygen (right alg.)
- → LeakyKeygen() can be simulated given an LWE sample $(\mathbf{A}, \mathbf{t}_0 = \mathbf{A} \mathbf{s}_0)$



⊳ Slow

⊳ Fast

⊳ Fast

⊳ Slow

⊳ No mask

Dilithium follows the Fiat-Shamir with aborts paradigm.

Sign(sk = s, vk = (A, t), msg) → sig Generate a short ephemeral secret r Compute the commitment w = A · r Compute the challenge c = H(w, msg, vk) Compute the response z = s · c + r Check that z is in a given interval. If not, restart. Signature is sig = (c, z)

Masking bottlenecks:

- 69 Short secret generation (1) requires B2A.
- 6 Rejection sampling (5) requires A2B.

Total masking overhead: $\Theta(d^2 \log q)$



$\mathsf{Sign}(\mathsf{sk} = [\![\textbf{s}]\!], \mathsf{vk} = (\textbf{A}, \textbf{t}), \mathsf{msg}) \to \mathsf{sig}$

1	Generate a masked short ephemeral secret $[\![\mathbf{r}]\!]$ using "AddRepNoise"	⊳ Fast
2	Compute the commitment $\llbracket \mathbf{w} \rrbracket = \mathbf{A} \cdot \llbracket \mathbf{r} \rrbracket$	⊳ Fast
3	Unmask [[w]] to obtain w	⊳ Fast
4	Compute the challenge $c = H(\mathbf{w}, msg, vk)$ \triangleright	No mask
6	Compute the response $[\![\mathbf{z}]\!] = [\![\mathbf{s}]\!] \cdot c + [\![\mathbf{r}]\!]$	⊳ Fast
6	Unmask [[z]] to obtain z	⊳ Fast
7	(No more rejection sampling!)	
8	Signature is $sig = (c, \mathbf{z})$	

Total masking overhead: $O(d \log d)$



$\mathsf{Sign}(\mathsf{sk} = [\![\textbf{s}]\!], \mathsf{vk} = (\textbf{A}, \textbf{t}), \mathsf{msg}) \to \mathsf{sig}$

1	Generate a masked short ephemeral secret [[r]] using "AddRepNoise"	⊳ Fast
2	Compute the commitment $[\![\mathbf{w}]\!] = \mathbf{A} \cdot [\![\mathbf{r}]\!]$	⊳ Fast
3	Unmask [[w]] to obtain w	⊳ Fast
4	Compute the challenge $c = H(\mathbf{w}, msg, vk)$ \triangleright	No mask
6	Compute the response $[\![\mathbf{z}]\!] = [\![\mathbf{s}]\!] \cdot c + [\![\mathbf{r}]\!]$	⊳ Fast
6	Unmask [[z]] to obtain z	⊳ Fast
7	(No more rejection sampling!)	
8	Signature is $sig = (c, \mathbf{Z})$	

Total masking overhead: $O(d \log d)$

But why would it even be secure?

Impact on the modulus





Impact on the modulus



 $m{0}$ Removing rejection sampling increases $\|m{r}\|/\|m{s}\|$ from $\Theta(\dimm{s})$ to $\Theta\left(\|c\|\sqrt{ ext{Queries}}
ight)$

Impact on the modulus



1 Removing rejection sampling increases $\|\mathbf{r}\| / \|\mathbf{s}\|$ from $\Theta(\dim \mathbf{s})$ to $\Theta(\|c\| \sqrt{\text{Queries}})$ **2** The increased *q* in turn requires increasing $\|\mathbf{s}\|, q/\|\mathbf{r}\|$ and/or the dimensions.





 \bigcirc With some tricks [SR23], RAM consumption is < 128 kB



Raccoon is a specific-purpose scheme aimed at high side-channel resistance:

- ☺ Same assumptions as Dilithium
- 🙂 Simpler
- Verification key size is similar
- 😮 Signature is 4x larger
- (2) When masked, orders of magnitude faster than other schemes are





Dmitri Asonov and Rakesh Agrawal.

Keyboard acoustic emanations.

In 2004 IEEE Symposium on Security and Privacy, pages 3–11. IEEE Computer Society Press, May 2004.

Melissa Azouaoui, Olivier Bronchain, Gaëtan Cassiers, Clément Hoffmann, Yulia Kuzovkova, Joost Renes, Tobias Schneider, Markus Schönauer, François-Xavier Standaert, and Christine van Vredendaal.

Protecting dilithium against leakage: Revisited sensitivity analysis and improved implementations.

IACR Transactions on Cryptographic Hardware and Embedded Systems, 2023(4):58–79, Aug. 2023.

Gilles Barthe, Sonia Belaïd, Thomas Espitau, Pierre-Alain Fouque, Benjamin Grégoire, Mélissa Rossi, and Mehdi Tibouchi.
 Masking the GLP lattice-based signature scheme at any order.
 In Jesper Buus Nielsen and Vincent Rijmen, editors, EUROCRYPT 2018, Part II, volume 10821 of LNCS, pages 354–384. Springer, Heidelberg, April / May 2018.

Jean-Sébastien Coron, François Gérard, Matthias Trannoy, and Rina Zeitoun. Improved gadgets for the high-order masking of dilithium. IACR Transactions on Cryptographic Hardware and Embedded Systems, 2023(4):110–145, Aug. 2023.

 Julien Devevey, Pouria Fallahpour, Alain Passelègue, and Damien Stehlé.
 A detailed analysis of fiat-shamir with aborts.
 In Helena Handschuh and Anna Lysyanskaya, editors, Advances in Cryptology – CRYPTO 2023, pages 327–357, Cham, 2023. Springer Nature Switzerland.

Wim Van Eck.

Electromagnetic radiation from video display units: An eavesdropping risk? *Computers & Security*, 4:269–286, 1985.

Thomas Espitau, Pierre-Alain Fouque, François Gérard, Mélissa Rossi, Akira Takahashi, Mehdi Tibouchi, Alexandre Wallet, and Yang Yu. Mitaka: A simpler, parallelizable, maskable variant of falcon. In Orr Dunkelman and Stefan Dziembowski, editors, EUROCRYPT 2022, Part III, volume 13277 of LNCS, pages 222–253. Springer, Heidelberg, May / June 2022.

Emre Karabulut and Aydin Aysu.

FALCON down: Breaking FALCON post-quantum signature scheme through side-channel attacks.

In 58th ACM/IEEE Design Automation Conference, DAC 2021, San Francisco, CA, USA, December 5-9, 2021, pages 691–696. IEEE, 2021.

- Paul C. Kocher, Joshua Jaffe, and Benjamin Jun.
 Differential power analysis.
 In Michael J. Wiener, editor, CRYPTO'99, volume 1666 of LNCS, pages 388–397.
 Springer, Heidelberg, August 1999.
- Paul C. Kocher.

Timing attacks on implementations of Diffie-Hellman, RSA, DSS, and other systems.

In Neal Koblitz, editor, *CRYPTO'96*, volume 1109 of *LNCS*, pages 104–113. Springer, Heidelberg, August 1996.

- Vincent Migliore, Benoît Gérard, Mehdi Tibouchi, and Pierre-Alain Fouque. Masking Dilithium - efficient implementation and side-channel evaluation. In Robert H. Deng, Valérie Gauthier-Umaña, Martín Ochoa, and Moti Yung, editors, ACNS 19, volume 11464 of LNCS, pages 344–362. Springer, Heidelberg, June 2019.
- Thomas Prest.

A key-recovery attack against mitaka in the *t*-probing model.

In Alexandra Boldyreva and Vladimir Kolesnikov, editors, *PKC 2023, Part I*, volume 13940 of *LNCS*, pages 205–220. Springer, Heidelberg, May 2023.

- Markku-Juhani O. Saarinen and Mélissa Rossi. Mask compression: High-order masking on memory-constrained devices. Cryptology ePrint Archive, Paper 2023/1117, 2023. https://eprint.iacr.org/2023/1117.
- Shiduo Zhang, Xiuhan Lin, Yang Yu, and Weijia Wang. Improved power analysis attacks on falcon. Cryptology ePrint Archive, Paper 2023/224, 2023. https://eprint.iacr.org/2023/224.